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Equalization system to improve the quality of bass sounds within a listening area

**Abstract**

Frequency equalization system substantially equalizes the room frequency responses generated by at least one loudspeaker within a listening area so that the frequency responses in the listening area are substantially constant and flat within a desired frequency range. The frequency equalization system uses multiple microphones to measure the impulse responses of the room and uses the impulse responses to design filters to process the audio signals of one or more subwoofers to achieve an improved bass response that is flat across the relevant frequency range. The system employs an algorithm that is a closed-form, non-iterative, mathematical solution and features very short computation time.

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## BACKGROUND OF THE INVENTION

### [0001] 1. Field of the Invention

[0002] This invention is generally directed to improving the quality of bass sounds generated by one or more loudspeakers within a listening area. More particularly, the invention is directed to substantially equalizing the responses generated by at least one loudspeaker within a listening area so that the responses in the area are substantially constant and flat within a desired frequency range.

### [0003] 2. Related Art

[0004] Sound systems typically include loudspeakers that transform electrical signals into acoustic signals. The loudspeakers may include one or more transducers that produce a range of acoustic signals, such as high, mid and low-frequency signals. One type of loudspeaker is a subwoofer that may include a low frequency transducer to produce low-frequency signals in the range of 20 Hz to 100 Hz.

[0005] The sound systems may generate the acoustic signals in a variety of listening environments. Examples of listening environments include, but are not limited to, home listening rooms, home theaters, movie theaters, concert halls, vehicle interiors, recording studios, and the like. Typically, a listening environment includes single or multiple listening positions for a person or persons to hear the acoustic signals generated by the loudspeakers. The listening position may be a seated position, such as a section of a couch in a home theater environment, or a standing position, such as a spot where a conductor may stand in a concert hall.

[0006] The listening environment may affect the acoustic signals, including the low, mid, and/or high frequency signals at the listening positions. Depending on the nature of the room and the position of a listener in a room and the position of the loudspeaker in the room, the loudness of the sound can vary for different frequencies. This may especially be true for low frequencies. Low frequencies may be important to the enjoyment of music, movies, and most other forms of audio entertainment. In the home theater example, the room boundaries, including the walls, draperies, furniture, furnishings, and the like may affect the acoustic signals as they travel from the loudspeakers to the listening positions.

[0007] The acoustic signals received at the listening positions may be measured. One method of characterizing the room is the impulse response of a loudspeaker to a microphone placed in the listening area. The impulse response is the acoustic signal measured by the microphone for a short sound burst emitted from the loudspeaker. The impulse response may allow measurement of various properties of the acoustical signals including the amplitude and/or phase at a single frequency, a discrete number of frequencies, or a range of frequencies.

[0008] An amplitude response is a measurement of the loudness at the frequencies of interest. Generally, the loudness or the amplitude is measured in decibels (dB). Amplitude deviations may be expressed as positive or negative decibel values in relation to a designated target value. The closer the amplitude values measured at a listening position are to the target values, the better the amplitude response is. Deviations from the target reflect changes that occur in the acoustic signal as it interacts with room boundaries. Peaks represent a positive amplitude deviation from the target, while dips represent a negative amplitude deviation from the target.

[0009] These deviations in the amplitude response may depend on the frequency of the acoustic signal reproduced at the subwoofer, the subwoofer location, and the listener position. A listener may not hear low frequencies as they were recorded on the recording medium, such as a soundtrack or movie, but instead as they were distorted by the room boundaries. Thus, the room can change the acoustic signal that was reproduced by the subwoofer and adversely affect the low-frequency performance of the sound system. As an example, FIG. 1 shows a sound system setup in a rectangular room. The sound system includes a receiver connected to four subwoofers, one at each corner of the room. The room is defined by four walls that can affect the low-frequency sound waves or bass sounds generated by the four subwoofers. Within the room, a seating area is provided to allow one or more persons to listen to the combined bass sound generated by each of the four subwoofers. A number of factors, as discussed above, can affect the quality of the sound within the listening area such that one person may hear a louder bass sound than another person sitting just a few feet away. For purposes of measuring the impulse response of the room, the receiver may send a logarithmic frequency sweep output signals to the four subwoofers for a predetermined amount of time. The impulse responses of the room are then picked up by four microphones P1, P2, P3, and P4 positioned at different locations within the listening area of the room.

[0010] FIG. 2 shows four frequency response curves F1, F2, F3, and F4, corresponding to the measured impulse responses one may expect at the four microphone positions P1, P2, P3, and P4, respectively. As discussed earlier, subwoofers generally operate in the low frequency range of between 20 Hz and 100 Hz. FIG. 2 indicates that at about 48 Hz, the magnitude or loudness of the bass sound varies in a wide range so that the loudness of the bass sound depends on where the person is located within the listening area. For instance, the curve F2 indicates that the bass loudness levels is about 0 dB at about 48 Hz, while the curve F3 indicates that the bass loudness level is about -18 dB, at the same frequency point. This means that a person sitting in location P2 hears a much louder bass sound at 48Hz than the person sitting just behind him at location P3. In other words, the sound level is not the same at different locations within the listening area of the room so that each person will experience a different bass sound quality. In addition, FIG. 2 shows that the curves fluctuate within the frequency range of interest. This means that certain bass sounds will drop off such that a person cannot hear the bass sound although it was intended to be heard. For instance, the curve F4 shows that between about 48 Hz and 55 Hz, there is a considerable drop in the bass loudness level at about 52 Hz. This means that a person sitting at location P3 will hear the bass sound at 48 Hz but notice a sudden drop in the bass sound at 52 Hz and a sudden peak again at 55 Hz. Such fluctuations in the bass sound level can impair the listening experience.

[0011] Many equalization techniques have been used in the past to reduce or remove amplitude deviations within a listening area. One of the techniques is spatial averaging that calculates an average amplitude response for multiple listening positions, and then equally implements the equalization for all subwoofers in the system. Spatial averaging, however, only corrects for a single "average listening position" that does not exist in reality. Thus, even when using spatial averaging techniques, some listening positions still have a better low-frequency performance than other positions but other locations may be severely affected. For instance, the spatial averaging may worsen the performance at some listening positions as compared to their un-equalized performance. Moreover, attempting to equalize and flatten the amplitude response for a single location potentially creates problems. While peaks may be reduced at the average listening position, attempting to amplify frequencies where dips occur requires significant additional acoustic output from the subwoofer, thus reducing the maximum acoustic output of the system and potentially creating large peaks in other areas of the room.

[0012] Another known equalization technique is to position multiple subwoofers in a "mode canceling" arrangement. By locating multiple loudspeakers symmetrically within the listening room, standing waves may be reduced by exploiting destructive and constructive interference. However, the symmetric "mode canceling" configuration assumes an idealized room (i.e., dimensionally and acoustically symmetric) and does not account for actual room characteristics including variations in shape or furnishings. Moreover, the symmetric positioning of the loudspeakers may not be a realistic or desirable configuration for the particular room setting.

[0013] Still another equalization technique is to configure the audio system in order to reduce amplitude deviations using mathematical analysis. One such mathematical analysis simulates standing waves in a room based on the room data. For example, room dimensions, such as length, width, and height of a room, are input and the various algorithms predict where to locate a subwoofer based on data input. However, this mathematical method does not account for the acoustical properties of a room's furniture, furnishings, composition, etc. For example, an interior wall having a masonry exterior may behave very differently in an acoustic sense than a wood framed wall. Further, this mathematical method cannot effectively compensate for partially enclosed rooms and may become computationally onerous if the room is not rectangular.

[0014] There are a number of other methods that try to equalize the impulse responses in a room but the accuracy of the equalization is more by chance because of the guessing involved in determining certain parameters such as delay and gain applied to the signals. As such, in order to obtain an accurate equalization solution, it takes a tremendous amount of computational power. Moreover, these methods do not provide an equalization that results in a flat frequency response within a desired low-frequency range so that loudness of the bass level is not only consistent at each seating location but also substantially constant or flat throughout the desired low-frequency range. Therefore, a long-standing need exists for a system to accurately determine a configuration for an audio system such that the audio performance for one or more listening positions in a given space is improved.

## SUMMARY

[0015] The invention addresses the widely known problem of low frequency equalization in a listening room. The invention is directed to a frequency equalization system that utilizes one or more microphones to measure the impulse responses of the room at various locations within a preferred listening area. This information is then used to filter the audio signals sent to the subwoofers in the room to improve the bass responses so that the frequency responses are substantially flat at the microphone measurement points and within the desired listening area, across the relevant frequency range.

[0016] The invention uses the impulse responses of the room to calculate coefficients to design a filter for each corresponding subwoofer so that the frequency responses are substantially flat within the listening area, across the relevant frequency range. In general, the inverses of the room responses are determined to undo the coloration added by the room. The inverses are smoothed so that sudden gains that may exceed the allowable gains that a subwoofer may handle are minimized or removed. The invention may also apply a target function on the inverse so that the equalization is applied to a desired frequency range in which the subwoofer optimally operates. The modified inverse is then used to determine the filter coefficient for each audio signal sent to its respective subwoofer. A processor such as a digital signal processor (DSP) may be used to filter the audio signal based on the filter coefficients.

[0017] Other systems, methods, features, and advantages of the invention will be, or will become, apparent to one with skill in the art upon examination of the following figures and detailed description. It is intended that all such additional systems, methods, features, and advantages be included within this description, be within the scope of the invention, and be protected by the following claims.

## BRIEF DESCRIPTION OF THE DRAWINGS

[0018] The invention can be better understood with reference to the following drawings and description. The components in the figures are not necessarily to scale, emphasis instead being placed upon illustrating the principles of the invention. Moreover, in the figures, like referenced numerals designate corresponding parts throughout the different views.

[0019] FIG. 1 shows a typical sound system setup in a rectangular room with a subwoofer in each corner of the room and a listening area defined by P1 through P4.

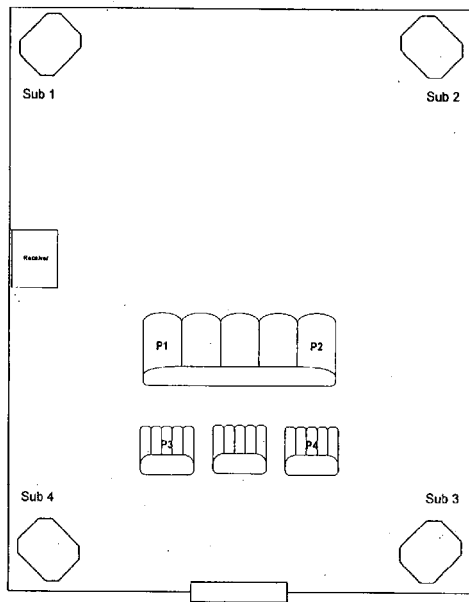


FIG. 1  
(PRIOR ART)

[0020] FIG. 2 shows four spectra F1, F2, F3, and F4, corresponding to the measured impulse responses one may expect at the four microphone positions P1, P2, P3, and P4, respectively.

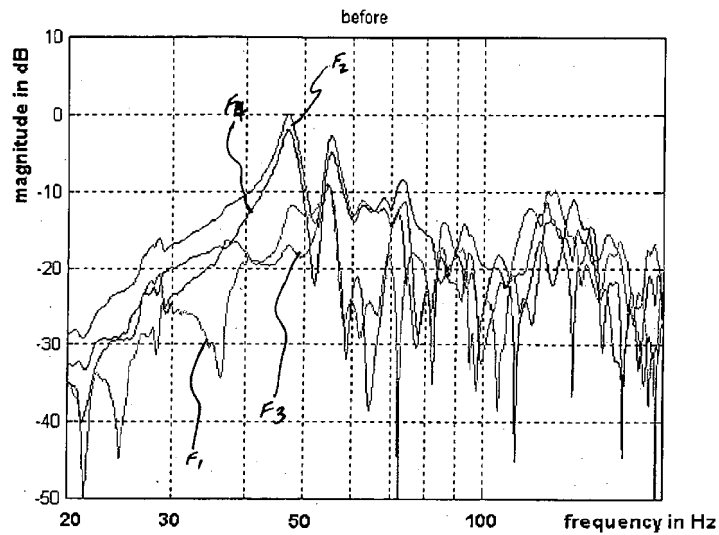


Fig. 2  
(PRIOR ART)

[0021] FIG. 3 shows a block diagram illustrating an equalization system in accordance with the invention.

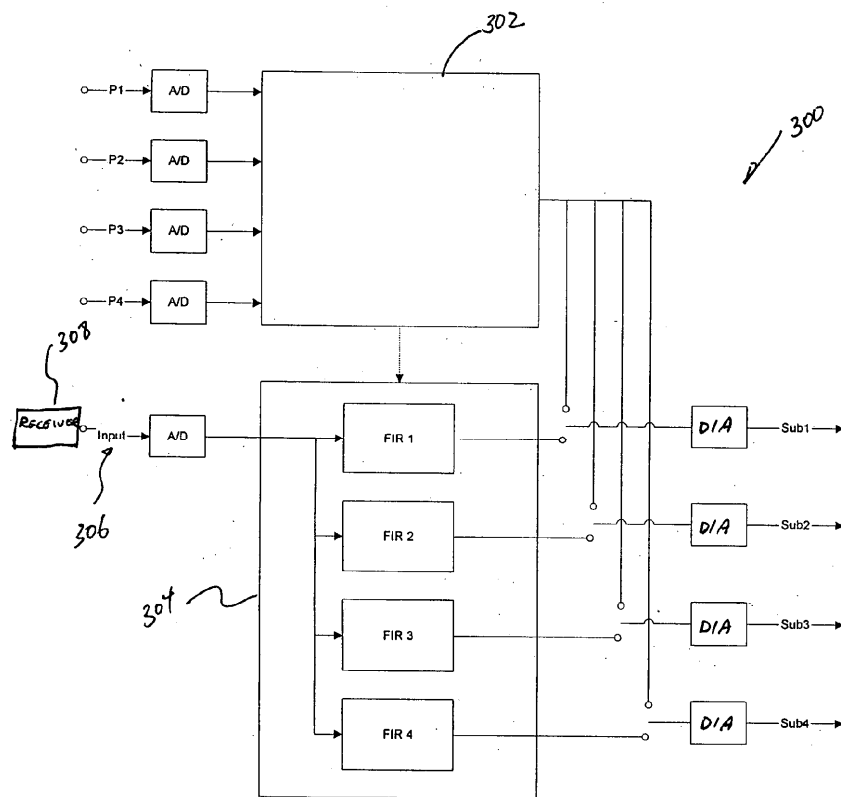


FIG. 3

[0022] FIG. 4 shows frequency responses of the room after the input signals to the corresponding subwoofers have been filtered to equalize the responses in accordance with this invention.

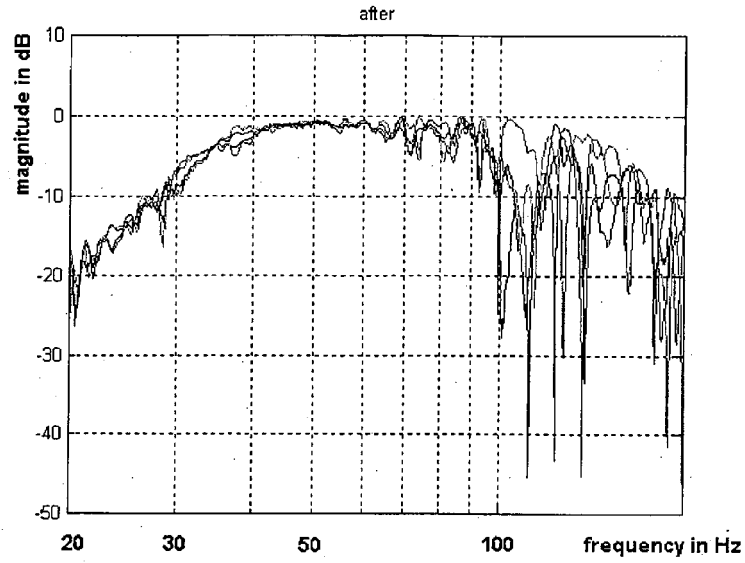


FIG. 4

[0023] FIG. 5 is a flow chart with an overview of the filter design procedure to equalize the frequency response of a room.

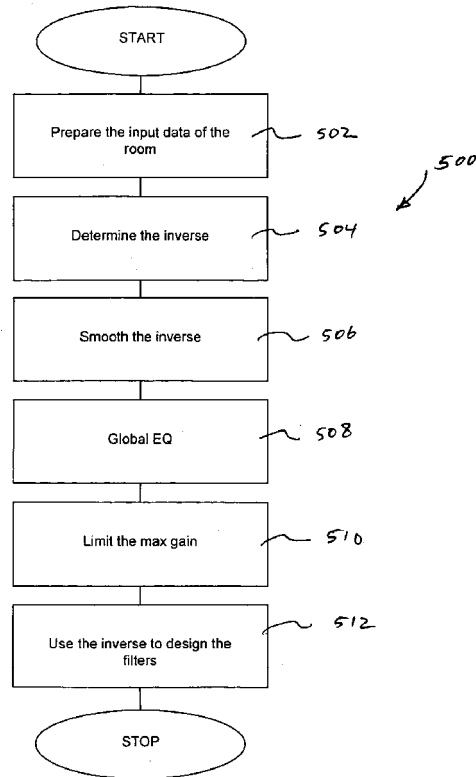


Fig. 5



[0024] FIG. 6 is a flow chart showing further details of preparing the input data step in FIG. 5.

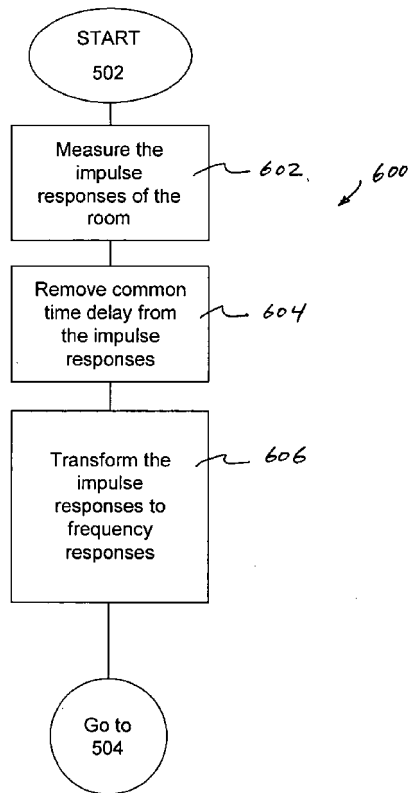


Fig. 6

[0025] FIG. 7 is a flow chart showing further details of determining the inversion for the frequency responses in FIG. 5.

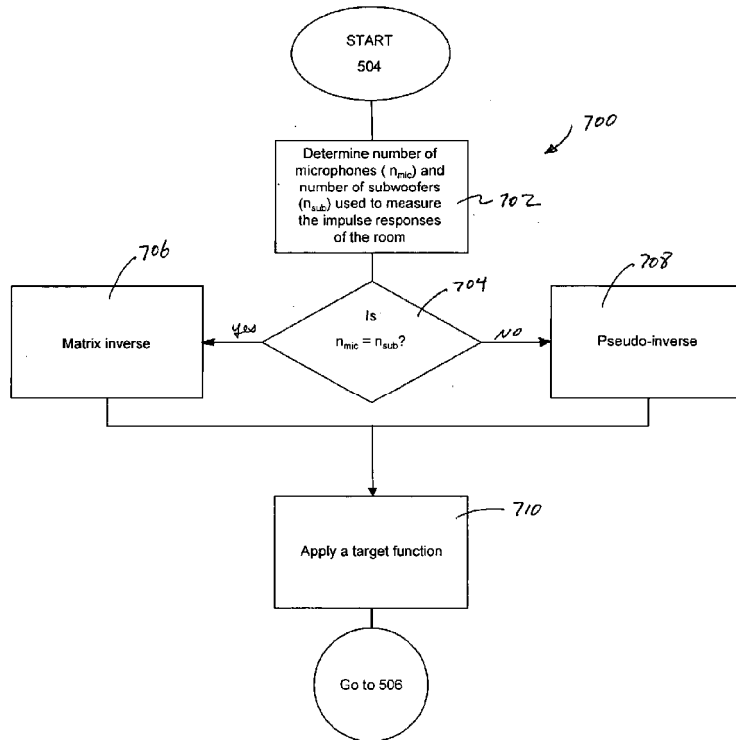


Fig. 7

[0026] FIG. 8 shows curves representing the inverse of the frequency responses.

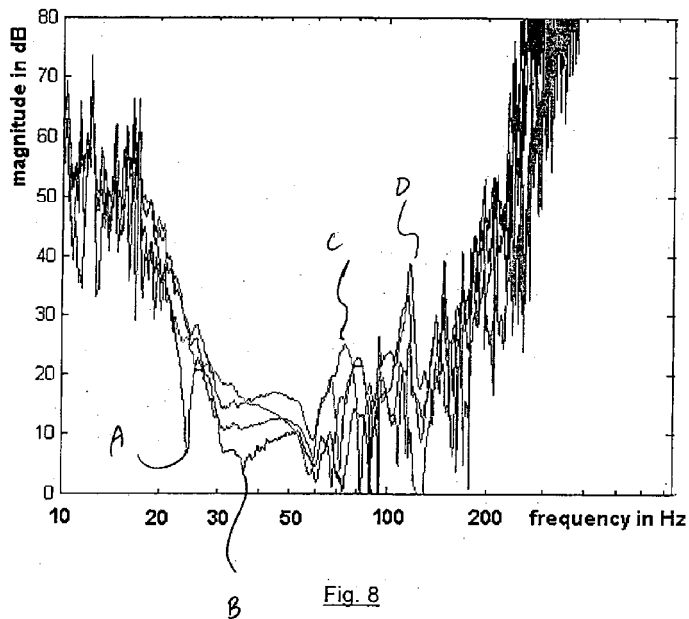


Fig. 8

[0027] FIG. 9 shows a curve  $F_s(2)$  representing the smoothed version of the curve  $F(2)$  in accordance with this invention.

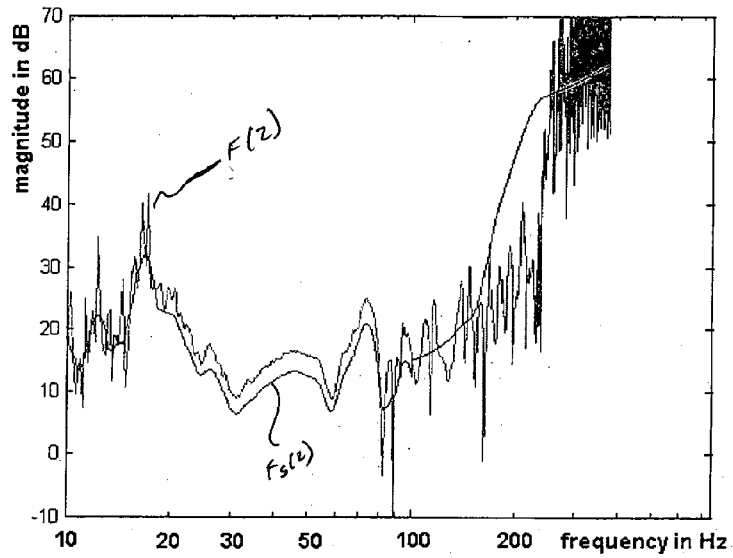


Fig. 9

[0028] FIG. 10 shows four curves  $F_s(1)$ ,  $F_s(2)$ ,  $F_s(3)$ , and  $F_s(4)$  representing the smooth version of the curves  $F(1)$ ,  $F(2)$ ,  $F(3)$ , and  $F(4)$  in FIG. 8, respectively.

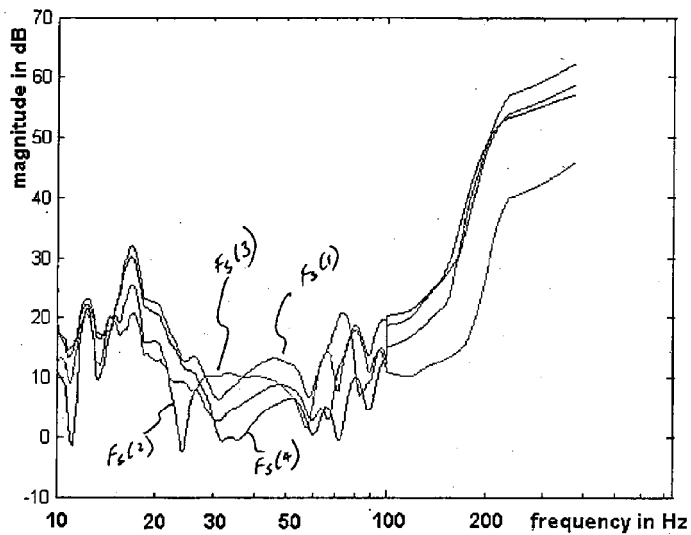


Fig. 10

[0029] FIG. 11 is a flow chart showing further details of determining the global equalization step in FIG. 5.

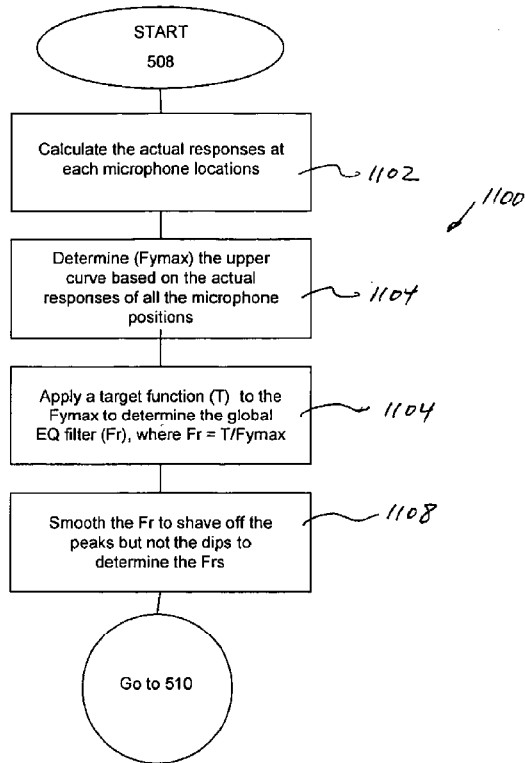


Fig. 11

[0030] FIG. 12 shows the frequency responses at the four microphone positions P1, P2, P3, and P4, after the filtering in accordance with the curves  $F_s(1)$ ,  $F_s(2)$ ,  $F_s(3)$ , and  $F_s(4)$ , respectively, shown in FIG. 10 have been applied.

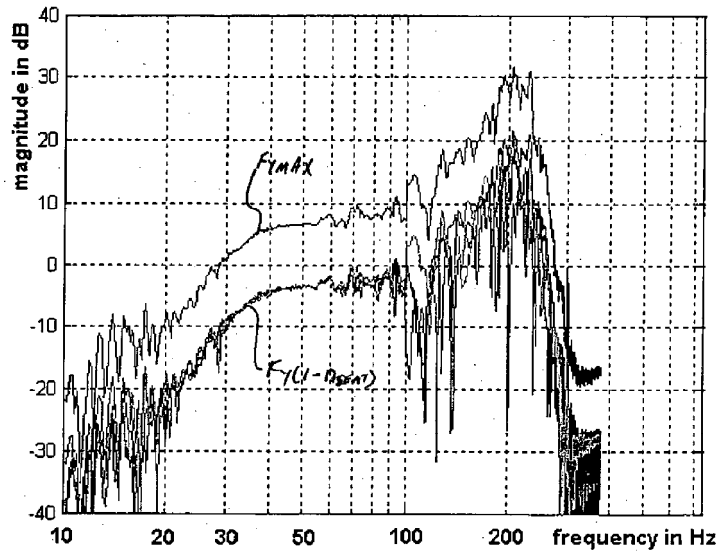
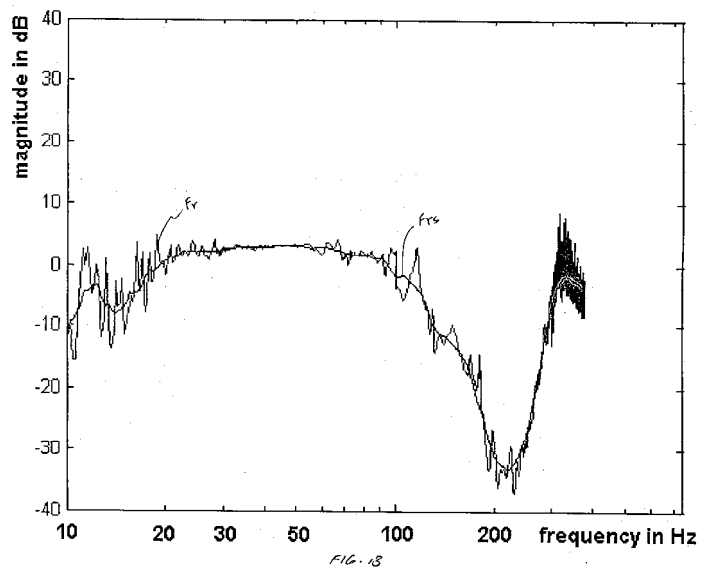
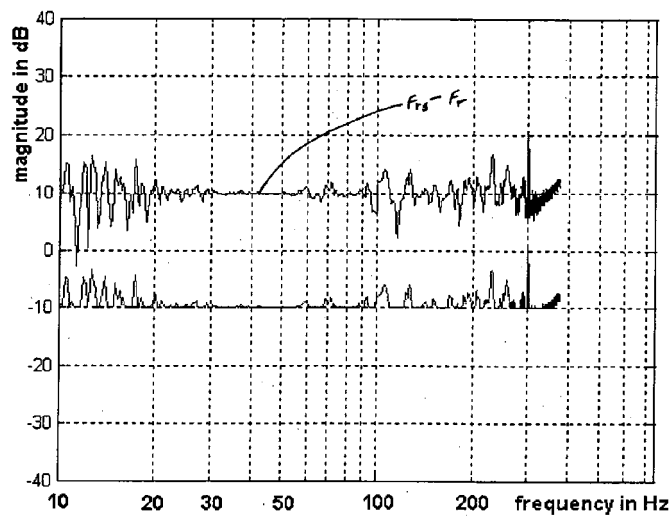


Fig. 12

[0031] FIG. 13 shows a global equalization filter that has been inverted.



[0032] FIG. 14 shows the top curve representing the difference between smoothed and unsmoothed frequency responses in FIG. 13, raised by 10 dB, and the lower curve representing the rectified difference (lowered by 10 dB).



[0033] FIG. 15 shows the final frequency response of global equalization filter.

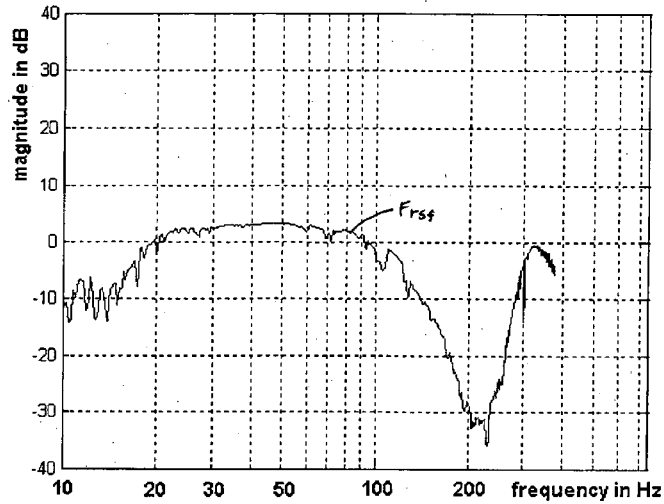


Fig. 15

[0034] FIG. 16 shows a flow chart further detailing the step of limiting the maximum gains in the global equalization filter as shown in FIG. 5.

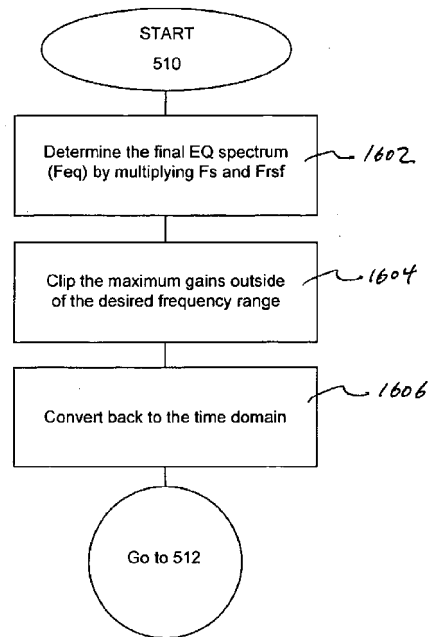


Fig. 16

[0035] FIG. 17 shows equalization filters for each of the subwoofers after complex smoothing of the curves  $F_s(1)$ ,  $F_s(2)$ ,  $F_s(3)$ , and  $F_s(4)$  shown in FIG. 10 and applying the global equalization filter shown in FIG. 15 to the smoothed curves of  $F_s(1)$ ,  $F_s(2)$ ,  $F_s(3)$ , and  $F_s(4)$ .

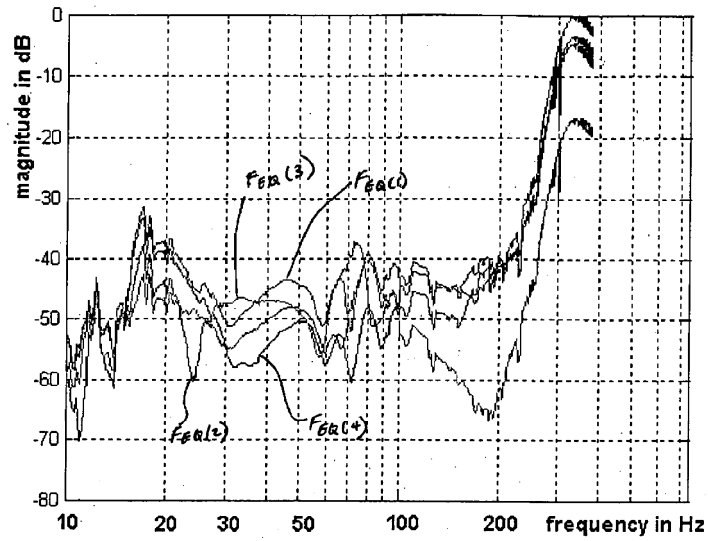


Fig. 17

[0036] FIG. 18 shows the filter EQ spectra after applying Maxgain and normalization to 0 dB as shown above.

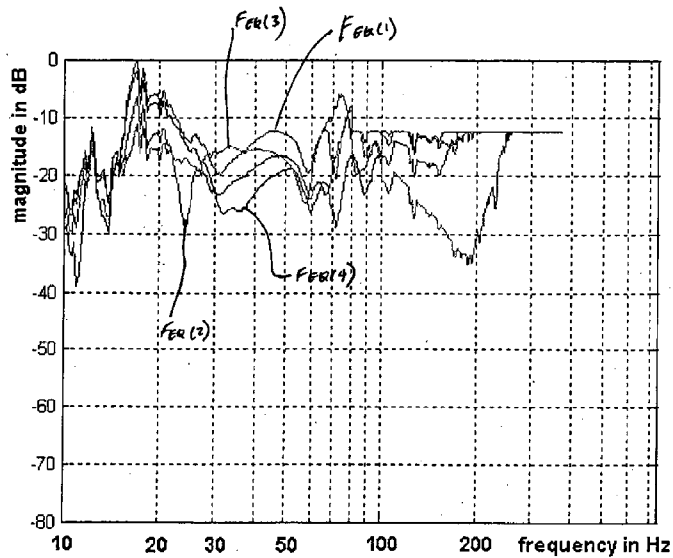


Fig. 18

[0037] FIG. 19 shows corresponding equalized impulse responses obtained for filter FIR1.

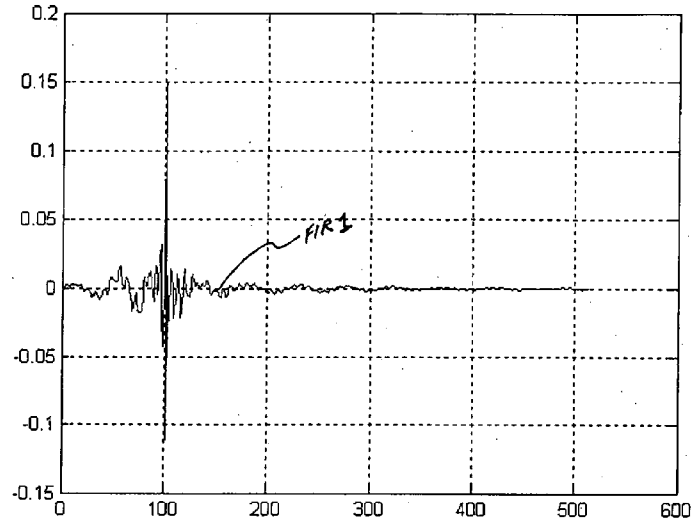


Fig. 19

[0038] FIG. 20 shows magnitude responses for the filters FIR1, FIR2, FIR3, and FIR4.

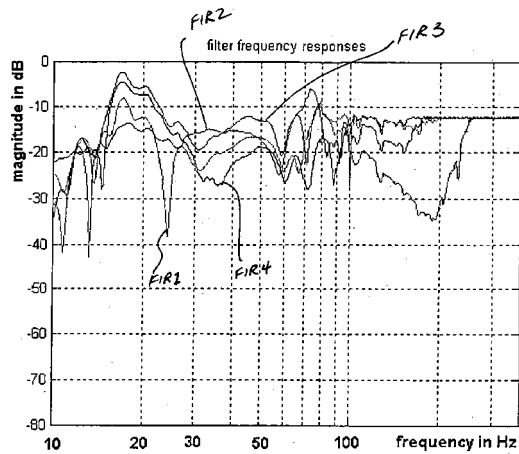


Fig. 20

### DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

[0039] FIG. 3 shows a block diagram illustrating an equalization system 300 in accordance with this invention, designed to achieve an improved bass response from one or more subwoofers within a room that is flat across a predetermined low-frequency range within a desired listening area of the room. The equalization system 300 may be used to equalize the frequency responses for a variety of rooms where each room has its own unique characteristics. For instance, a room may have one or more of the following characteristics: (1) one or more walls of the room may be open; (2) a ceiling or walls of the room may have an arc; (3) drapes may cover one or more walls of the room; (4) the



floor of the room may be uneven; (5) there may be one or more subwoofers in the room; (6) location of each of the subwoofers may be positioned anywhere in the room, and etc. As such, the equalization system 300, as described in detail below, may be used to equalize the frequency responses for any room.

[0040] For purposes of this discussion, the equalization system 300 (EQ system 300) is used to equalize the responses for the room illustrated in FIG. 1. The room is generally defined by four walls forming a rectangular configuration. Within the room, there is a seating area to allow one or more persons to sit as defined by positions P1, P2, P3, and P4. The seating area generally defines the listening area of the room. A receiver 308 may be located within the room to send audio signals to the subwoofers and incorporate the equalization system 300.

[0041] The EQ system 300 includes a signal block 302 that is capable of generating test signals and designing the coefficients for each filter corresponding to the loudspeaker in the room. In this example, the signal block 302 is linked to the four subwoofers Sub1, Sub2, Sub3, and Sub4 located in each corner of the room. The signal block 302 may send out output signals one at a time to each of the four subwoofers to measure the impulse response of that subwoofer to each of the microphones P1 through P4 placed in the room. The signal block 302 may output a logarithmic frequency sweep for a predetermined amount of time sequentially to each of the subwoofers. The logarithmic frequency sweep allows the signal block 302 to send out an output signal covering a broad frequency spectrum of interest through the subwoofers. As an example, the output signals may be sent out for about four seconds.

[0042] With each of the subwoofers sending out output signals over for a period of time, the impulse responses may be measured independently or simultaneously by the microphones located in different areas of the room ("listening positions") such as positions represented by P1 through P4 in FIG. 1. For instance, the signal block 302 may send an output signal through the Sub1 so that the microphones may measure the impulse response of the room from the signals generated in the upper-left corner of the listening area. The signal block 302 may then send another output signal through the Sub2 so that the microphones may measure the impulse response of the room due to the output signal source generated from the upper-right corner of the listening area. Likewise, an output signal may be sent through the Sub3 and another through the Sub4 so that the microphones may measure the impulse responses due to the subsequent separate signals sent from the bottom-right and bottom-left corners of the listening area, respectively. In this example, four subwoofers placed in the four corners of a rectangular room and four microphones placed within a desired listening area of the room are used to measure the impulse responses of the room. The microphones P1 to P4 convert the acoustic signals into electrical signals. Before the electrical signals are provided to the signal block 302, the electrical signals may be digitized at the predetermined rate using the A/D converter.

[0043] Through the microphones, the signal block 302 may capture a predetermined number of impulse response samples per second for each combination of subwoofer and microphone. The captured impulse responses may be down-sampled to yield N samples

for each measured impulse response. With four subwoofers and four microphones, this results in a set of sixteen impulse responses where each set has N number of samples. For example, the signal block 302 may capture  $N=2048$  samples at a sampling rate of 750 samples per second.

[0044] The signal block 302 receives the measured impulse responses of the room from the microphones P1 through P4. The signal block 302 calculates the filter coefficients, as described below, based on the impulse responses of the room. The signal block 302 is linked to a processor block 304 that implements the designed filters as calculated pursuant to the invention to modify each of the audio signals sent to the corresponding subwoofer to substantially equalize the in-room frequency responses due to the sound generated by the four subwoofers. In this example, the processor block 304 may filter four audio signals represented by FIR1, FIR2, FIR3, and FIR4, as shown in FIG. 3, corresponding to each of the subwoofers Sub1, Sub2, Sub3, and Sub4, respectively. As such, the audio signal input 306 provided by a variety of sources 308 such as a TV, DVD player, audio receiver, and the like, is processed by the processor block 304 through the corresponding filters FIR1 through FIR 4 so that the output signal sent to its respective subwoofer is filtered in accordance with the filter coefficients to equalize the frequency responses of the room. The processor block 304 may be a variety of processors such as a digital signal processor (DSP), and the filter may be a Finite Impulse Response (FIR) filter. Note that it is within the scope of this invention to have one processor perform the functions done by the signal block 302 and processor block 304.

[0045] FIG. 4 shows frequency responses of the room shown in FIG. 1, after the output signals to the subwoofers have been filtered to equalize the responses pursuant to the subject invention. FIG. 4 shows that the resulting amplitude responses are substantially consistent in the low frequency range relative to each other. This indicates that the responses at different locations within the listening room are substantially constant. This means that each person within the listening area is provided with a substantially similar loudness level at each frequency point. In addition, the magnitude level is substantially constant or flat across a desired low-frequency level of between about 40 Hz and about 100 Hz so that sound level dropping off is substantially minimized. Comparing FIG. 4 to FIG. 2, the amplitude responses of the room have been substantially improved. The following is a detailed discussion of how filters are designed for each of the subwoofers pursuant to this invention.

[0046] The following discussion is for the specific case of four subwoofers and four microphones, i.e.,  $n_{sub.sub}=4$ , and  $n_{sub.mic}=4$ , within a room as shown in FIG. 1. However, this invention can be used for any combination of subwoofers and microphones in a room. The audio signal sent to one or more subwoofers may be filtered in accordance with the following description.

[0047] FIG. 5 is a flow chart with an overview of the filter design procedure to equalize the frequency response of a room. In block 502, the input data may be prepared to substantially equalize the frequency responses of the room. Preparing the data generally includes measuring the impulse responses of the room and transforming them into

frequency domain. In the block 504, an inverse for each of the frequency responses may be determined. Each of the inverses would in effect undo the coloration added by the walls of the room. In other words, filtering each of the audio signals with its respective inverse and sending the filtered signals to their respective subwoofers would produce ideal frequency responses. The inverse, however, may have local sudden peaks and dips where such sudden gains may exceed the allowable gains that a subwoofer may handle. As such, in block 506, the local peaks and dips in the inverse may be smoothed using a complex smoothing method described in more detail below. This provides approximate inverses for the frequency responses of the room.

[0048] In block 508, global equalization is applied to the result after approximate inverse filtering, so that a target function describing transitions at the low and high frequency band edges may be approximated. The global equalization also uses a smoothing method that addresses peaks and dips separately, as described below. As subwoofers generally operate below 100 Hz, in block 510, a limit may be placed on the gain that may be applied to the subwoofer outside of the desired low-frequency range to protect the subwoofer, such as below 20 Hz and/or above 100 Hz. In block 512, the inverse of the global equalization is then used to determine the filter to process each of the audio signals sent to each of the subwoofers to substantially equalize the frequency responses of the room.

[0049] FIG. 6 is a flow chart 600 showing further details of preparing the input data for the room as represented in block 502 in FIG. 5. Preparing the input data includes block 602 that measures the impulse responses of the room, as discussed above. In block 602, once the impulse responses have been measured, in block 604, any common time delay from the impulse responses may be removed. This is done to allow the solvability of the mathematical problem of complex smoothing discussed below. For instance, with regard to the output signal sent by the Sub1, as shown in FIG. 1, located in the upper-left corner of the room, the microphone P1 is closest to the Sub1. As such, the microphone P1 will receive the output signal from the Sub1 before the other microphones. The time it takes for the output signal from the Sub1 to reach the microphone P1 is common to other microphones P2-P4. This time may be defined as a common time delay with regard to the impulse responses measured by the four microphones P1-P4 for the output signal sent by the Sub1. Likewise, a corresponding common time delay may be measured for output signals sent by each of the other Sub2-Sub4. For instance, a common time delay for the output signal sent by the Sub3 is the time it takes for the output signal from the Sub3 to reach its closest microphone P4. The minimum delay of all the measured impulse responses is the common time delay. The common time delay may be offset or deducted from all the impulse responses measured by the four microphones.

[0050] In block 606, the input data of the time domain impulse responses of the room, may be transformed into frequency domain using Fast Fourier Transform (FFT). In FIG. 1 for example, there are four microphones and four loudspeakers so that a set of sixteen impulse responses may be measured where each set has N number of samples. Each impulse response is transformed into frequency domain using FFT. In this example, an N point FFT is employed that yields N complex values for each measured impulse response.

As such, the resulting set of  $[n_{\text{sub.mic}} \times n_{\text{sub.sub}}] \times N$  complex FFT points are represented as  $N$  number of  $n_{\text{sub.mic}} \times n_{\text{sub.sub}}$  matrices  $A_{\text{sub.i}}$ , where  $i=1 \dots N$ . At each  $i$  or frequency point, the FFT provides amplitude and phase.

[0051] FIG. 7 is a flow chart 700 further detailing the method of determining the inverse of the frequency responses as represented by the block 504 in FIG. 5. In block 702, the number of microphones  $n_{\text{sub.mic}}$  used to measure the impulse responses and the number of subwoofers  $n_{\text{sub.sub}}$  in the room are determined. In decision block 704, if  $n_{\text{sub.mic}}=n_{\text{sub.sub}}$ , then in block 706, exact matrix inversion method may be used to find the exact inverse of the impulse responses. On the other hand, if  $n_{\text{sub.mic}}>n_{\text{sub.sub}}$ , then, in block 708, pseudo-inverse method may be used to find the inverse of the impulse responses. In FIG. 1, four microphones and four subwoofers are used to measure the impulse response so that exact matrix inversion method is used to calculate the inverse. With the impulse responses transformed into the frequency domain in the block 604, the inverse matrices may be calculated at each of the frequency points to determine the ideal equalization at that frequency point. In this regard,  $N$  number of inverse matrices  $B_{\text{sub.i}}$ , where  $i=1 \dots N$ , may be determined. This results in  $N$  complex-valued matrices  $B_{\text{sub.i}}$ , such that  $A_{\text{sub.i}} B_{\text{sub.i}}=1$ .

[0052] In the case that  $n_{\text{sub.mic}}>n_{\text{sub.sub}}$ , the method of pseudo-inverse may be used to calculate  $B_{\text{sub.i}}$ . The well-known method of pseudo-inverse minimizes the mean squared error between the desired and actual result. Expressed mathematically,  $B_{\text{sub.i}}$  is computed such that  $(1-A_{\text{sub.i}}B_{\text{sub.i}})^* \cdot (1-A_{\text{sub.i}}B_{\text{sub.i}})$  is minimized where  $*$  denotes a complex-conjugate operation.

[0053] In block 710, once the inverse matrices have been determined, a target function may be chosen for each frequency point for each of the microphone positions P1 through P4. The target function is the desired frequency response at each listening position. The target function may be a complex-value vector containing  $n_{\text{sub.mic}}$  elements  $T_{\text{sub.i}}$  ( $i=1 \dots N$ ). In this example of four microphones,  $T_{\text{sub.i}}$  contains four complex-valued elements per frequency point. A simple example of target  $T_{\text{sub.i}}$  is a unity vector. The vectors  $F_{\text{sub.i}}$  that describes  $n_{\text{sub.sub}}$  filters at a particular frequency point  $i$  ( $i=1 \dots N$ ), are then computed as matrix multiplication  $F_{\text{sub.i}}=B_{\text{sub.i}}T_{\text{sub.i}}$ . The vectors  $F_{\text{sub.i}}$  describe filters at a particular frequency point  $i$  ( $i=1 \dots N$ ), that would perform an exact inverse (ideal equalization). The vectors  $F_i$  in effect undo the coloration added by the walls of the room so that multiplying  $A_{\text{sub.i}}F_{\text{sub.i}}=A_{\text{sub.i}}B_{\text{sub.i}}T_{\text{sub.i}}=T_{\text{sub.i}}$  results in an idealized equalization.

[0054] FIG. 8 is a graph showing the logarithmic magnitude of the filters  $F(k)$  ( $k=1 \dots n_{\text{sub.sub}}=4$ ) as obtained after the matrix inversion. The target function used in this example may be a unity vector  $T_{\text{sub.i}}=[1 \ 1 \ 1 \ 1]$ ,  $i=1 \dots N$ . The frequency axis  $f$  is  $f=(1 \dots N/2)/N \cdot f_a$ , where  $N$  is FFT length and  $f_a=750$  Hz is the sampling frequency. FIG. 8 shows that there are sudden peaks and dips as indicated by markings A, B, C, and D, for example. Directly applying the filters  $F(k)$  to the output signals sent to the Sub1-Sub4 to equalize the frequency responses within the room may damage the subwoofers because the peaks at certain frequencies require applying significant gains at those frequencies

that may be too high for the subwoofers to handle. In other words, the vectors  $F(k)$  may impose gains at certain frequencies that may exceed the maximum amount of gain that the subwoofers can handle.

[0055] Smoothing throughout the whole frequency range may be done to limit the length of the resulting filter in the time domain, which is known to converge to zero more rapidly after smoothing. The following is further discussion of smoothing the inverse of the matrices represented by the block 506 in FIG. 5. With the sudden peaks and dips in the frequency response vectors  $F(k)$ , the ideal equalization may not be directly applied to the output signal sent to the subwoofers. The peaks and dips in the vectors  $F(k)$ , however, may be minimized by smoothing the complex-value vectors  $F(k)$  across frequency. This may be accomplished through the method described in an article entitled "Generalized Fractional-Octave Smoothing of Audio and Acoustic Responses," by Panagiotis D. Hatziantoniou and John N. Mourjopoulos, published April of 2000, J. Audio Eng. Soc., Vol. 48, No. 4, pp 259-280. In particular, smoothing of the complex-valued vectors  $F(k)$  may be carried out by computing the mean values separately for the real and imaginary parts, along a sliding frequency-dependent window, resulting in  $F_s(k)$ . For example, a smoothing index  $q$  between 1.0 and 2.0 may be used, where  $i^{*(q-1/q)}$  denotes the width of the frequency-dependent sliding window. Sliding windows such as Hanning or Welch window may be used. Note that it may be useful to perform smoothing in two or more separate frequency bands by using a different value for each frequency band. At higher frequencies, fluctuations across space and frequency in a room are usually larger, so that a higher  $q$  index may be used. Since the subwoofer operates mainly below 80 Hz, a high accuracy of the inversion filter above that frequency may not be necessary, and not even desirable, because it may not apply to the whole listening area consistently, due to rapid fluctuations.

[0056] FIG. 9 shows the magnitude of the unsmoothed spectrum of the filter  $F(2)$  that may be applied to the output signal sent to the Sub2, and curve  $F_s(2)$  representing the smoothed version of filter  $F(2)$  with the method discussed above. Note that in curve  $F_s(2)$  local peaks and dips are smoother than in curve  $F(2)$  such that much of the sudden peaks and dips present in curve  $F(2)$  are more gradual in curve  $F_s(2)$ . As such, curve  $F_s(2)$  is an approximation of the complex-valued filter  $F(2)$  so that equalization may be applied to the output signal to the Sub2 without the local excessive gain. Likewise, FIG. 10 shows curves of the magnitude responses of all four filters after smoothing, i.e.,  $F_s(1)$ ,  $F_s(2)$ ,  $F_s(3)$ , and  $F_s(4)$ .

[0057] FIG. 11 shows a flow chart 1100 further detailing the method of determining the global equalization as represented by the block 508 in FIG. 5. The complex smoothing of each of the complex-valued filters  $F(1)$  through  $F(4)$  removes the local fluctuations of peaks and dips but the extreme gains may be still present. For example, subwoofers are generally designed to handle a maximum gain of about 15 db to about 20 db. FIG. 9 shows a gain of about 30 db below 20 Hz and a gain of about 60 db above 100 Hz. Such extreme gains may not be handled by the subwoofers.

[0058] To manage the gains, a global equalization (EQ) may be performed. One of the

ways of calculating the global EQ is through the method described in FIG. 11. In block 1102, the actual responses at each of the microphone positions or seats  $F_y(j)$  ( $=1 \dots n.sub.seat$ ) may be calculated by multiplying the original matrix  $A$  with  $F_s$ , (calculated in the above smoothing method). In other words,  $F_y=A*F_s$ . FIG. 12 shows the responses at the four microphone positions (listener seats), after the (intermediate) filters of FIG. 10 have been applied. In block 1104, an upper curve  $F_{ymax}$  may be determined by taking the maximum magnitudes  $Max\{F_y(1 \dots n.sub.seat)\}$  for each frequency points. As such, all of the responses at the seats are below the curve  $F_{ymax}$ . FIG. 12 shows the curve  $F_{ymax}$  raised by 10 dB to better show the  $F_{ymax}$  curve. This means that no response is greater than the curve  $F_{ymax}$  along any frequency point.

[0059] The curve  $F_{ymax}$  denotes the maximum magnitudes in dB within the whole frequency range of 0 Hz to half the sample rate. Subwoofers, however, are design to operate optimally in a more limited range than the above frequency range. As such, in block 1106, the upper curve  $F_{ymax}$  may be limited within a predetermined frequency range that would allow the subwoofers to operate at their optimal frequency range. In this regard, a global EQ filter  $F_r$  may be computed to operate in the predetermined frequency range by dividing a target function  $T$  by  $F_{ymax}$  or  $F_r=T/F_{ymax}$ . The target function  $T$  is real-valued having magnitude frequency responses of high pass and low pass filters that characterize the frequency range where the respective transducer (subwoofer) optimally works. Typical filters are Butterworth high passes of order  $n=2 \dots 4$  (corner frequencies 20 . . . 40 Hz), and Butterworth low passes of order  $n=2 \dots 4$ , corner frequencies 80 . . . 150 Hz.

[0060] FIG. 13 shows the log-magnitude response of the global EQ filter  $F_r$ . FIG. 13 shows that the response has peaks that may interfere with the quality of the sound. In this regard, in block 1108, the peaks in the curve  $F_r$  may be removed through the following method. The smoothing method described above may be used to determine an intermediate response  $F_{rs}$  that is the smoothed version of  $F_r$ . The peaks in  $F_r$  in essence may be "shaved off" by computing the difference between  $F_{rs}$  and  $F_r$ , and rectifying the difference. FIG. 14 shows the top curve representing the difference between  $F_{rs}$  and  $F_r$  (raised by 10 db), and the lower curve representing the rectified difference (lowered by 10 db). Then, as shown in FIG. 15, the final frequency response of the global EQ filter  $F_{rsf}$  may be obtained by subtracting the rectified difference from the original filter  $F_r$  that is the unsmoothed filter shown in FIG. 13. The final  $F_{rsf}$  shown in FIG. 15 shows dips but a reduced number of peaks. The unwanted peaks would attempt to amplify frequencies where dips occur in the original response, requiring significant additional acoustic output from the subwoofer, thus reducing the maximum acoustic output of the system and potentially creating large peaks in other areas of the room.

[0061] FIG. 16 shows a flow chart 1600 further detailing the method of limiting the max gain on the global EQ curve as represented by the block 510 in FIG. 5. In block 1602, the final EQ spectrum  $F_{eq}$  is computed by multiplying the complex spectra  $F_s$  of the individual EQ filters, as determined above, with the global, real-valued magnitude spectrum  $F_{rsf}$  (as determined above), respectively. FIG. 17 shows EQ filters obtained after complex smoothing and global EQ. FIG. 17 shows that there are still substantial

gains above 200 Hz and below about 20 Hz. This may be due to the chosen target function that is not sufficient to limit the final gains as desired. Therefore, in block 1604, limits may be put on the gains below a predetermined low frequency and a predetermined high frequency. For example, a limit on the maximum gain may be applied by replacing the complex-valued  $F_{eq}$  such that the maximum magnitude is clipped to `Maxgain` without altering the phase. Maxgain is a value prescribed by the user that depends on the capabilities of the particular subwoofer. Preferably, different values of Maxgain can be applied in different frequency bands. The resulting filters may be scaled so that the maximum gain does not exceed one (0 dB). FIG. 18 shows the filter EQ spectra after applying Maxgain and normalization to 0 dB as shown above. The EQ spectra is normalized to 0 dB to maximize the average gain.

[0062] In block 1606, the final EQ filter frequency responses may be converted back to the time domain by using inverse FFT, resulting in coefficients of Finite Impulse Response (FIR) filters. A time window may be applied to the coefficients to limit the filter length. FIG. 19 shows the impulse response of one of the obtained FIR filters (filter FIR 1). FIG. 20 shows magnitude responses of the resulting filters FIR1, . . . , FIR4. FIG. 4, as discussed above, shows the resulting responses at the four seats P1 through P4 after applying the obtained EQ filters. Note that within the target frequency range, such as between about 40 Hz and 80 Hz, the responses are consistent and flat to provide a substantial equalization within that frequency range. This means that a person sitting in any one of the locations P1 through P4 will hear a substantially similar loudness level of the bass sound. In other words, the sound level is substantially same at different locations within the listening area of the room so that each person will experience same bass sound quality. In addition, FIG. 4 shows that the curves are substantially flat within the frequency range of interest. This means that bass sounds will be substantially consistent within that desired frequency range so that there is minimal, if any, drop off in bass sound within the desired frequency range.

[0063] The equalization system described above may be used for a variety of rooms having different configurations with at least one subwoofer. The room may comprise any type of space in which the loudspeaker is placed. The space may have fully enclosed boundaries, such as a room with the door closed or a vehicle interior; or partially enclosed boundaries, such as a room with a connected hallway, open door, or open wall; or a vehicle with an open sunroof. In addition, a room may be an open area such as a field or a stadium with a closed or open top. Low-frequency performance in a space will be described with respect to a room in the specification and appended claims; however, it is to be understood that vehicle interiors, recording studios, domestic living spaces, concert halls, movie theaters, partially enclosed spaces, and the like are also included. Room boundaries, such as room boundary walls, include the partitions that partially or fully enclose a room. Room boundaries may be made from any material, such as gypsum, wood, concrete, glass, leather, textile, and plastic. In a home, room boundaries are often made from gypsum, masonry, or textiles. Boundaries may include walls, draperies, furniture, furnishings, and the like. In vehicles, room boundaries are often made from plastic, leather, vinyl, glass, and the like. Room boundaries have varying abilities to reflect, diffuse, and absorb sound. The acoustic character of a room boundary may affect

the acoustic signal.

[0064] The loudspeakers may come in a variety of shapes and sizes. For instance, a loudspeaker may be enclosed in a box-like configuration housing the transducer. The loudspeaker may also utilize a portion of the wall or vehicle as all or a portion of its enclosure. The loudspeaker may provide a full range of acoustical frequencies from low to high. Many loudspeakers have multiple transducers in the enclosure. When multiple transducers are utilized in the loudspeaker enclosure, it is common for individual transducers to operate more effectively in different frequency bands. The loudspeaker or a portion of the loudspeaker may be optimized to provide a particular range of acoustical frequencies, such as low frequencies. The loudspeaker may include a dedicated amplifier, gain control, equalizer, and the like. The loudspeaker may have other configurations including those with fewer or additional components.

[0065] A loudspeaker or a portion of a loudspeaker including a transducer that is optimized to produce low-frequencies is commonly referred to as a subwoofer. A subwoofer may include any transducer capable of producing low frequencies. Loudspeakers capable of producing low frequencies may be referred to by the term subwoofer in the specification and appended claims; however, any loudspeaker or portion of a loudspeaker capable of producing low frequencies and responding to a common electrical signal is included.

[0066] The measurement devices such as microphones may communicate with other electronic devices such as the signal block 302 in order to measure acoustic signals in various parts of a room. The measured acoustic signal output from the different loudspeaker locations for the different listening positions may be stored, such as on the external disk. The external disk may be input to the computational device. The computational device may be another computing environment and may include many or all of the elements described above relative to the measurement device. The computational device may be incorporated into an audio/video receiver located within a room or remotely located to process the impulse responses at a different location than the room.

[0067] While various embodiments of the invention have been described, it will be apparent to those of ordinary skill in the art that many more embodiments and implementations are possible within the scope of this invention. Accordingly, the invention is not to be restricted except in light of the attached claims and their equivalents.

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